Model and Chattering Free Adaptive Fuzzy SMC for Robotic Manipulator Systems

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Annotation: This In recent decades, many researchers proposed fuzzy Sliding Mode Control (SMC) strategies that aim to eliminate the chattering problem in control of Multi-Input-Multi-Output (MIMO) nonlinear robotics manipulator systems. All these methods impose the need to determine the dynamic model of system under control, which is a challenging task in many practical cases. This paper presents a new model free and chattering free SMC method for MIMO nonlinear robotics manipulator systems based on Proportional-Derivative (PD) and fuzzy logic control. Proposed controller combines the robustness feature of SMC, simplicity of Proportional-Integral-Derivative (PID) control and ability of fuzzy technique in function approximation of discontinuity part of traditional SMC. In this paper, PD control is used as equivalent control in order to stabilize the system while adaptive fuzzy SMC is used to handle uncertainty of the system. Lyapunov's second method is utilised to prove stability of proposed controller. Two different robotic manipulator configurations; two-links with payload and three links robotic manipulator under external disturbance and system uncertainties are simulated to demonstrate the efficiency of the proposed method.

Keywords: SMC, Robotics Systems, Fuzzy Control, Trajectory Tracking, lyapunov stability

1. Introduction

The complexity of the robot manipulator dynamic, high nonlinearities and strong coupling are making trajectory control task of these systems very difficult [1-5]. Moreover, most of these systems are suffering from system uncertainties and external disturbance which increase the difficulty of the motion control of the robot manipulator systems. Different control schemes had been proposed for this problem such as model predictive control, feedback linearization, and computed torque control. However, these control approaches are model based which means that the dynamic of robot manipulator must be known and this may be difficult in practical applications. Proportional integral derivative (PID) controllers are still widely used in the industrial application due to simplicity in its structure and also in tuning its parameters ([2,3]. Modern control strategies combined with PID controller to increase its ability to dealing with parameter variations, uncertainties and external disturbance for controlling nonlinear systems like robot manipulator. Adaptive control, neural control, and robust control are the most control schemes that used with PID to improve its performance and ensuring its stability and convergence of tracking error for controlling nonlinear systems([4-12]. Sliding mode control is one of the most important nonlinear robust control techniques that applied successfully in control of multivariable nonlinear systems in presence of external disturbance and system uncertainties. The traditional SMC control law consists of two terms, first one is equivalent control term that is based on dynamic model of controlled system and the second one is referred to as discontinuous control. There are two main drawbacks related with traditional SMC. In practical applications, it may not be easy to determine the exact dynamic model of the system due to uncertainties and complexity of system structure; and discontinuous term causes the high frequency chattering problem[13-21]. Chattering can be reduced by using saturation function instead of signum function or by employing a low pass filter in practice. The ability of ANN to approximate the nonlinear function is exploited and used in representation of system dynamics to approximate the sliding mode equivalent control[22]. Based on the method proposed by Roopaei and Jahromi in 2009 that eliminates chattering of SMC, and control scheme presented in[23] that avoids the need to determine dynamic model of

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robotic manipulator, this paper proposes a novel control scheme for general MIMO nonlinear robotic manipulator systems that is simple and robust. The main advantages of proposed method are: i) guaranteed robust behaviour of controlled system in presence of system uncertainties and external disturbance; ii) model free design procedure with the control law being based only on error, its derivative and sliding surface; and iii) removal of the chattering problem. This paper is organized as follows: Sec.2 discusses the robotic manipulator dynamic model. Sec. 3 presents the proposed control method. Stability of the proposed method by Lyapunov's second method discussed in Sec.4. in Sec. 5, the theoretical results are used for controlling two links and three link SCARA robot arms and compares its performance with standard SMC subjected to parameter variations and external disturbance. Conclusions are included in Sec.6.

2. Robotic Manipulator Dynamic

Dynamic model of a MIMO nonlinear robotic manipulator system can be expressed as follows:

$$M(q)\ddot{q} + N(q,\dot{q})\dot{q} + G(q) + H(\dot{q}) + \tau_d = \tau \tag{1}$$

Where $q \in \mathbb{R}^n$ is joint angular position vector, τ is torque vector, $M(q) \in \mathbb{R}^{n \times n}$ is inertia matrix as a function of q, $N(q, \dot{q}) \in \mathbb{R}^{n \times n}$ is Coriolis/centripetal vector, $G(q) \in \mathbb{R}^n$ is gravity vector, $H(\dot{q}) \in \mathbb{R}^n$ is frictional force vector and $\tau_d \in \mathbb{R}^n$ is external disturbance. In general, the system dynamics and external disturbance are unknown but they are known to be bounded. The following properties and assumptions about robot dynamics are required [9].

Property 1. Symmetry and boundedness of M(q):

(2)	
(3)	
(4)	
(5)	
(6)	
(7)	
(t) are bounded as follows:	llows:
	 (2) (3) (4) (5) (6) (7) (t) are bounded as formation (1)

with M_{d1i} , M_{d2i} , and M_{d3i} being positive constants.

3. Proposed Control Scheme

In order to overcome the shortcoming mentioned above, an adaptive FSMC method is proposed as follows (Structure of proposed control scheme is depicted in Fig. 1:



Figure 1 Proposed control scheme

$$\tau = u_{eq} - u_r \tag{8}$$

Where

$$u_{eq} = k_p E + k_d \dot{E} \tag{9}$$

$$u_r = k_r u_f \tag{10}$$

$$E^{T} = [e_{1} \cdots e_{n}] = [q_{1d} - q_{1} \cdots q_{nd} - q_{n}]$$
(11)

E is the tracking error, k_r represents the normalization factor of output variable and its positive definite diagonal matrix , and u_f is the output of fuzzy SMC (FSMC). k_p and k_d are proportional and derivative positive definite diagonal matrix respectively. Robust control law in (8) is designed as follows:

$$u_{f} = FSMC(S(t), \dot{S}(t))$$

$$= [FSMC(s_{1}(t), \dot{s}_{1}(t)), \cdots, FSMC(s_{n}(t), \dot{s}_{n}(t))]^{T}$$
(12)

$$s_{i}(t) = c_{i}e_{i}(t) + \dot{e}_{i}(t)$$
(13)

$$S = [s_{1}, s_{2}, \cdots, s_{n}]^{T} = CE + \dot{E}$$
(14)

$$C = diag(c_{1}, c_{2} ..., c_{n})$$
(15)

Where $s_i(t)$ are the sliding surfaces and c_i are positive constants. $FSMC(S(t), \dot{S}(t))$ refers to the characteristics of fuzzy decision system that is mapping the input linguistic variables S(t), $\dot{S}(t)$ to the output variable u_f . The membership functions used are triangular as shown in Fig.2 and they are decomposed into seven fuzzy sets expressed as NB (Negative Big), NM (Negative Medium), NS (Negative Small), Z (Zero), PS (Positive Small), PM (Positive Medium) and PB (Positive Big). 49 fuzzy rules shown in Table 1 are used and intersection minimum and centre average operations are used for fuzzification and

defuzzification, respectively. To improve the performance of closed-loop system and reduce the required control effort, reaching control gain k_r can be tuned according to the distance of states to the sliding surface. The fuzzy rules of supervisory system that are used to adjust k_r are developed with one normalized input variable s(t) and one normalized output variable k_f where $k_r = k.k_f$. k is a positive definite diagonal matrix and $k_f = diag(k_{f1}, ..., k_{fn})$ is decomposed into four normalized fuzzy sets of Z (Zero), S (Small), M (Medium), and B (Big). The membership functions of inputs and outputs linguistic variables are shown in Fig. 3



Figure 2 Fuzzy sets for the input variables k_{fi} and output variables $s_i(t)$, $\dot{s}_i(t)$

Table 1 49 fuzzy rules

Du(t)		s(t)						
		NL	NM	NS	NE	PS	PM	PL
Ds(t)	NL	NL	NL	NL	NL	NM	NS	ZE
	NM	NL	NL	NL	NM	NS	ZE	PS
	NS	NL	NL	NM	NS	ZE	PS	PM
	NE	NL	NM	NS	ZE	PS	PM	PL
	PS	NM	NS	ZE	PS	PM	PL	PL
	PM	NS	ZE	PS	PM	PL	PL	PL
	PL	ZE	PS	PM	NL	PL	PL	PL



Figure 3 Fuzzy sets for the output variable k_{fi}

The following rules are used to tune k_{fi} :

1) If $s_i(t)$ is NB or PB then k_{fi} is B,

2) If $s_i(t)$ is NM or PM then k_{fi} is M,

(17)

3) If $s_i(t)$ is NS or PS then k_{fi} is S,

4) If $s_i(t)$ Z then k_{fi} is Z.

4. Stability Analysis

Stability analysis of proposed control is executed using Lyapunov's second method with the following positive definite Lyapunov function candidate and its derivative:

$$V = \frac{1}{2}S^T M(q)S \tag{16}$$

$$\dot{V} = S^T M \dot{S} + \frac{1}{2} S^T \dot{M} S = S^T M \dot{S} + S^T N S$$

The dynamic model of the robotic manipulator is linearly parameterized and can be expressed in terms of a nominal reference, \dot{q}_r [3].

$$Y\phi = M(q)\ddot{q}_{r} + N(q,\dot{q})\dot{q}_{r} + G(q) + H(\dot{q})$$
(18)
$$\dot{q}_{r} = \dot{q}_{d} + C(q_{d} - q)$$
(19)

where $Y = Y(q, \dot{q}, \dot{q}_r, \ddot{q}_r) \in \mathbb{R}^{n \times p}$ is the dynamic regression matrix that contains a known nonlinear function, $\emptyset \in \mathbb{R}^p$ is a vector that contains unknown constant parameters and α is a positive diagonal matrix.

$$V = S^{T}[M(q)(\ddot{q}_{r} - \ddot{q}) + N(q, \dot{q})(\dot{q}_{r} - \dot{q})]$$
(20)
= $S^{T}[M(q)\ddot{q}_{r} + N(q, \dot{q})\dot{q}_{r} + G(q) + H(\dot{q}) + \tau_{d} - \tau$ (21)
 $\dot{V} = S^{T}[Y\phi + \tau_{d} - \tau]$ (22)

According to properties (2-6) and the result in [12] that stand for bounded desired trajectory q_d ,

$$||Y\phi|| < \rho(t)$$
, where $\rho(t)$ is a state-dependent function.

$$\begin{split} \dot{V} &\leq \|S\| [\rho(t) + D^{+}] - S^{T} \tau \end{aligned}$$
(23)

$$\dot{V} &\leq \|S\| [\rho(t) + D^{+} + S^{T} [-k_{p}E - k_{d}\dot{E} + k_{r}u_{f}] \end{aligned}$$
(24)

$$\dot{V} &\leq \|S\| [\rho(t) + D^{+}] + S^{T} [-k_{d} (k_{d}^{-1} k_{p}E + \dot{E}) + k_{r}u_{f}] \end{aligned}$$
(25)
If we select $C = k_{d}^{-1}k_{p}$, then (25) becomes

$$\dot{V} &\leq \|S\| [\rho(t) + D^{+}] + S^{T} [-k_{d}S + k_{r}u_{f}] \end{aligned}$$
(26)
Let $\delta(t) = \rho(t) + D^{+}$. Fuzzy rules [1] in Table 1 are selected such that $s_{i}u_{fi} = -|s_{i}|$, then

$$S^{T} u_{r} = -[|s_{1}| + \dots + |s_{n}|] = -\|S\| \end{aligned}$$
(27)

With a centroid defuzzification method used for tuning k_r , the minimum value for k_r is

with a centroid defuzzification method used for tuning
$$k_r$$
, the minimum value for k_r
 $k_r^{min} = 0.1 k^{min}$ (28)
where
 $k^{min} = \min(k)$
 $\dot{V} \le \delta(t) ||S|| - ||k_d| ||S||^2 - k_r^{min} ||S||$ (30)
 $\dot{V} \le [||\delta(t)|| - k_r^{min}] ||S|| - ||k_d| ||S||^2$ (31)

If we select $k_r^{min} > ||\delta(t)||$, then $\dot{V} \le 0$, As a result, the nonlinear system under proposed control is globally stable and tracking error converges to zero.

5. Simulation Results

(29)

(40)

This section demonstrates the effectiveness of the proposed control method via simulation tests. Two different robot manipulators used in this simulation: two links arm with payload and three links CSARA robot to illustrate generality and effectiveness of the proposed method. In order to demonstrate the effectiveness of proposed scheme, it is compared with conventional SMC. Integral Absolute Error (*IAE*) criterion is used to evaluate effectiveness of control schemes.

$$IAE = \int_0^{tf} |e(t)| dt \tag{32}$$

5.1 Two links robotic manipulator with payload

The following dynamic mode of the two links arm is used in this simulation [24]:

$$\begin{bmatrix} \tau_1 \\ \tau_{21} \end{bmatrix} = \begin{bmatrix} A_{11} & A_{12} \\ A_{12} & A_{12} \end{bmatrix} \begin{bmatrix} \ddot{q}_1 \\ \ddot{q}_2 \end{bmatrix} + \begin{bmatrix} -b\dot{q}_2 & -b\dot{q}_1 - b\dot{q}_2 \\ b\dot{q}_1 & 0 \end{bmatrix} \begin{bmatrix} \dot{q}_1 \\ \dot{q}_2 \end{bmatrix} + \begin{bmatrix} v_1\dot{q}_1 \\ v_2\dot{q}_2 \end{bmatrix} + \begin{bmatrix} p_1sgn(\dot{q}_1) \\ p_2sgn(\dot{q}_2) \end{bmatrix} + \begin{bmatrix} G_1 \\ G_2 \end{bmatrix}$$
(33)

$$A_{11} = I_1 + I_2 + m_1 l_{c1}^2 + m_2 [l_1^2 + l_{c2}^2 + 2l_1 l_{c2} \cos(q_2)] + m_p [l_1^2 + 2l_1 l_2 \cos(q_2) + l_2^2]$$
(34)

$$A_{12} = I_2 + m_2 [l_1 l_{c2} \cos(q_2) + l_{c2}^2] + m_p [l_1 l_2 \cos(q_2) + l_2^2]$$
(34)
$$A_{12} = A_{21}$$
(35)

$$A_{22} = I_2 + m_2 l_{c2}^2 + m_p l_2^2 \tag{36}$$

$$b = m_2 l_1 l_{c2} \sin(q_2) \tag{37}$$

$$G_2 = m_2 l_{c2} g \cos(q_1 + q_2) \tag{38}$$

where q_1 and q_2 are angular positions, τ_1 and τ_2 are torques, l_1 and l_2 are lengths, I_1 and I_2 are lengthwise centroid inertia, l_{c1} and l_{c2} are distances from the joint, m_1 and m_2 are masses, v_1 and v_2 are coefficients of viscous friction, and p_1 and p_2 are coefficients of dynamic friction of Link1 and Link2, respectively. The parameters of the robotic manipulator are selected as $m_1 = 1 kg$, $m_2 = 1 kg$, $l_1 = 1$, $l_2 = 1$, $l_{c1} = .5 m$, $l_{c2} = .5 m$, $l_1 = .2 kg m^2$, $l_2 = .2 kg m^2$ $P_1 = P_2 = .1$, $V_1 = V_2 = 0.1$. The desired joint trajectories in this simulation are selected as $q_d(t) = [q_{d1} q_{d2}]^T$, where

$$q_{d1} = 0.3 + 0.1\sin(t) \tag{39}$$

$$q_{d2} = 0.4 + 0.1\cos(t)$$

The controller parameters selected as follows:

 $k_d = diag(22,22), k_p = diag(55,55)$ and k = diag(50,50). To demonstrate the robustness and effectiveness of the proposed control method, the dynamic model of the robot manipulator is subjected to external disturbance and also model uncertainties. Moreover, it's compared with the SMC as shown in Figures 4 and 5. In this simulation the parameters of the robot manipulator which include mass, constant friction, and dynamic friction of Link1 and Link2 are changed as much as 15% of their nominal values with disturbance signal d = 5sin(3t). These figures indicate clearly that the performance of the proposed control method is better than SMC and also with smaller position tracking errors with respect to SMC. Moreover, these figures indicate clearly faster response of the proposed method. The input torque signals of Link1 and, Link2 are shown in Figures 4-c and 5-c. It can be seen form these figures that the same control effort payed form the two methods except a small duration of time at the beginning. Finally, superiority of the proposed control scheme with respect to SMC is approved by calculating *IAE* as shown in Table 3 that lists the *IAE* values. This table shows that ability of the proposed control method to reduce tracking error.

5.2 Three Links SCARA Robot

The dynamic model of the three link robot manipulator used is as follows [25]:

$$\begin{bmatrix} \tau_1 \\ \tau_2 \\ \tau_3 \end{bmatrix} = \begin{bmatrix} D_{11} & D_{12} & 0 \\ D_{12} & D_{22} & 0 \\ 0 & 0 & D_{33} \end{bmatrix} \begin{bmatrix} \ddot{q}_1 \\ \ddot{q}_2 \\ \ddot{q}_3 \end{bmatrix} + \begin{bmatrix} C_{11} & C_{12} & 0 \\ C_{21} & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} \dot{q}_1 \\ \dot{q}_2 \\ \dot{q}_3 \end{bmatrix}$$

$$+ \begin{bmatrix} v_1 \dot{q}_1 \\ v_2 \dot{q}_2 \\ v_3 \dot{q}_3 \end{bmatrix} + \begin{bmatrix} p_1 sgn(\dot{q}_1) \\ p_2 sgn(\dot{q}_2) \\ p_3 sgn(\dot{q}_3) \end{bmatrix} + \begin{bmatrix} G_1 \\ G_2 \\ G_3 \end{bmatrix} + \begin{bmatrix} D_1 \\ D_2 \\ D_3 \end{bmatrix}$$
(41)

$$D_{11} = \frac{1}{3}l_1^2 m_1 + \left[l_1^2 + l_1 l_2 \cos(q_2) + \frac{1}{3}l_2^2\right] m_2 + (l_1^2 + 2l_1 l_2 + l_2^2)m_3$$
(42)

$$D_{12} = -\left(\frac{1}{2}l_1l_2\cos(q_2) + \frac{1}{3}l_2^2\right)m_2 - (l_1l_2 + l_2^2)m_3 \tag{43}$$

$$D_{22} = \frac{1}{3}l_2^2 m_2 + l_2^2 m_3 \tag{44}$$

$$C_{11} = -l_1 l_2 \sin(q_2) \,\dot{q}_2 m_2 - 2l_1 l_2 \sin(q_2) \,\dot{q}_2 m_3 \tag{45}$$

$$C_{12} = -\frac{1}{2}l_1l_2\sin(q_2)\dot{q}_2m_2 - l_1l_2\sin(q_2)\dot{q}_2m_3$$
(46)

$$C_{21} = -\frac{1}{2} l_1 l_2 \sin(q_2) \,\dot{q}_1 m_2 - l_1 l_2 \sin(q_2) \,\dot{q}_1 m_3 \tag{47}$$

where q_1 , q_2 and q_3 are angular positions, τ_1 , τ_2 and τ_3 are torques, l_1 , l_2 and l_3 are lengths, m_1 , m_2 and m_3 are masses, v_1 , v_2 and v_3 are coefficients of viscous friction, and p_1 , p_2 and p_3 are coefficients of dynamic friction of Link1, Link2 and Link3, respectively.



Figure 4. two link tracking position (a), tracking error (b), input torque (c) of link 1





Figure 6 three link tracking position (a), tracking error (b), input torque (c) of link 1



Figure 7 three link tracking position (a), tracking error (b), input torque (c) of link 2



Figure 8. three link racking position (a), tracking error (b), input torque (c) of link 3

The parameters of the robotic manipulator are selected as $m_1 = 1 kg$, $m_2 = 0.8 kg$, $m_3 = 0.5 kg$, $P_1 = P_2 = P_3 = 12$, $V_1 = V_2 = V_3 = 0.2$ [14]. The desired joint trajectories in this simulation are selected as $q_d(t) = [q_{d1} \ q_{d2} \ q_{d3}]^T$

where

$$q_{d1} = 0.3 + 0.1\sin(t) + .3\sin(1.7t) + .2\sin(2.9t)$$
(48)
(67)

$$q_{d2} = 0.4 + 0.1\cos(t) + .3\sin(2.9t) + .2\sin(3.7t)$$
(49)

$$q_{d3} = 0.1 + 0.1\sin(t) + .2\sin(1.8t) + .3\sin(3.7t)$$
(50)

The controller parameters selected for this manipulator as follows:

$$k_d = diag(30,30,30), k_p = diag(500,500,500), k = diag(500, 500,500)$$

Parameters of the robot manipulator dynamic are changed to 14% of their nominal values with external disturbance d = 5sin(3t).

The simulation results that obtained when the proposed method and SMC used for controlling three links SCARA robot manipulator conform the result that obtained when two link robot manipulator used in the test. Tracking position and tracking error for link1, link2 and link3 are shown in Figures 2,3 and 4 respectively. These figures show faster response of the prosed method and also very small position error with respect the SMC which can be also justified based on the *IAE* values that listed in the Table 3. Figures 2,3 and 4 show the control signals for the Link1, Link2 and Link3 respectively.

6. Conclusion

In this paper, a model and chattering free adaptive fuzzy SMC scheme for nonlinear robotic manipulator systems with uncertainty in system dynamics in presence of the external disturbance has been proposed. The proposed control method does not require determining the dynamic model of the controlled system with adaptive switching gain to eliminate the chattering problem. Proposed scheme's performance is justified and compared it with the standard SMC by applying them for controlling two links and three links SCARA robot arm.

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